

1 ARC*: A Tool to Rate AI Models for Robustness Through a Causal 2 Lens for Enabling Trustworthy Model Selection 3 4

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Abstract

15 AI models are widely used in web applications and data-driven
16 services that rely on continuously collected and evolving online
17 data. Their decisions can be affected by bias, noise, and shifts in
18 the underlying data. This paper presents ARC, an interactive web-
19 based tool for rating AI models for robustness using causality-
20 based methods. ARC quantifies robustness, encompassing fairness
21 and stability, through causal metrics that measure how predictions
22 vary with perturbations and protected attributes, and allows users
23 to explore trade-offs between robustness and accuracy. The tool
24 is model-agnostic and task-independent: users can upload their
25 own datasets or select from four supported domains including
26 binary classification, sentiment analysis, group recommendation,
27 and time-series forecasting, and evaluate multiple models under a
28 shared causal setup. ARC helps developers assess models trained or
29 deployed on web data and supports informed model selection. The
30 demonstration video is available at <https://tinyurl.com/bd3cxhrb>.
31

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1 Introduction

2 AI models increasingly shape user experiences in decision support,
3 recommendation, and information systems that rely on web-scale
4 or user-generated data. Their growing use in such settings, where
5 models are retrained or adapted using online data streams, has
6

7 *ARC stands for AI Rating through Causality.
8

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33 renewed concerns about transparency and bias [1, 21, 25]. Most systems
34 remain black boxes that learn correlations rather than causal
35 relations [10], limiting interpretability and trust [22, 23]. Early work
36 introduced rating methods for bias by analyzing how model outputs
37 vary with protected attributes. This idea was demonstrated
38 for translation APIs, chatbots, and search engines [2, 28, 29, 31],
39 showing that bias can be quantified alongside performance without
40 access to model internals. Related studies on fairness in ranking
41 and recommender systems [4, 8, 24] further emphasized the need
42 for systematic evaluation of model behavior in web and data-driven
43 contexts. Yet most existing approaches rely on statistical definitions
44 such as parity or equalized odds [11, 35, 37], which help quantify
45 bias but not its underlying cause.
46

47 Causal analysis provides a way to assess how changes in input
48 or protected attributes affect model outcomes [5, 7, 30]. Our
49 earlier work applied this idea to rating AI models for robustness
50 [13, 27] across sentiment analysis [17], composite tasks [14], and
51 time-series forecasting [15, 16], though each was treated separately.
52 We define robustness as comprising three dimensions: sensitivity
53 to confounders that create spurious correlations between input and
54 output, sensitivity to changes in protected attributes, and sensitivity
55 to perturbations in input attributes. Building on these works, **ARC**
56 unifies causal evaluation across tasks, allowing users to explore
57 trade-offs between accuracy and robustness through *Pareto frontiers*
58 and to upload their own datasets for computing metrics and ratings
59 within the same interface.
60

61 **Key benefits of ARC:** (a) provides a single interface for
62 applying causal robustness metrics across different AI tasks;
63 (b) enables exploration of accuracy-robustness trade-offs
64 through Pareto frontiers; and (c) supports user-supplied datasets
65 for evaluating model outcomes using ARC's built-in metrics.
66 We contribute (1) a general, extensible tool for rating AI models
67 through causal analysis; (2) demonstrations across four tasks: binary
68 classification, sentiment analysis, group recommendation, and
69 time-series forecasting, showing its generalizability; and (3) discussion
70 of how the resulting ratings and Pareto frontiers enable informed
71 model selection.
72

2 Problem

73 In this section, we introduce the generalized causal model used by
74 ARC and the key research questions it addresses. The formulation
75 provides a unified view of how robustness and accuracy can be
76 jointly analyzed through causal reasoning. Such a formulation is
77 particularly relevant for web-scale and data-driven AI systems,
78

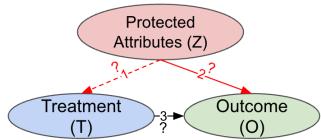


Figure 1: Generalized causal model used by ARC. The validity of link (1) depends on the conditional distribution $p(O | T, Z)$, while links (2) and (3) are tested using ARC’s metrics.

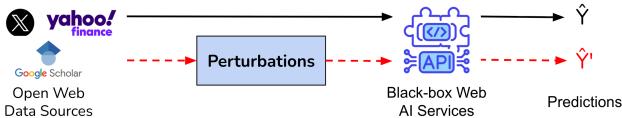


Figure 2: Data-to-predictions workflow showing how open web data sources are processed and passed through black-box AI services to obtain unperturbed and perturbed predictions (\hat{Y} and \hat{Y}'), which form the input for ARC’s causal evaluation.

where models are often used as black boxes and evaluated only through observed input-output behavior.

ARC assumes that model predictions \hat{Y} depend on a treatment variable T (representing different input conditions or perturbations) and may be indirectly affected by protected attributes Z such as gender or age. The observed outcome O , for example, prediction accuracy or residual error, varies with T and can also depend on Z . The causal model M (Figure 1) captures these relationships. If Z influences both T and O , it introduces a *confounding effect*, creating a backdoor path that biases the estimated effect of T on O . Backdoor adjustment methods [9, 19, 36] are used to isolate the true causal effect, denoted by $p(O | do(T))$. In the figure, solid arrows represent testable causal links evaluated through ARC’s metrics, while the dotted arrow indicates a potential indirect dependence between T and Z . The framework helps answer four central research questions: **RQ1:** Does Z influence O , even when Z has no effect on T ? Measures the statistical bias exhibited by the model. **RQ2:** Does Z affect the relationship between T and O when Z influences T ? Measures confounding bias that arises when protected attributes alter how treatments affect outcomes. **RQ3:** Does T affect O when Z may also influence O ? Measures the causal effect of treatments on outcomes while controlling for protected attributes, capturing robustness under varying conditions. **RQ4:** Does T affect the accuracy of the model? Measures model performance across treatment conditions.

3 System Demonstration

3.1 Workflow Overview

Figures 2 and 3 show the prerequisite *data-to-predictions* stage and the main ARC *predictions-to-ratings* stage. The first stage represents how data from open web sources such as *Yahoo! Finance* or *Google Scholar* are processed through black-box AI models to obtain predictions on both unperturbed (\hat{Y}) and perturbed (\hat{Y}') inputs. These pairs form the evaluation data for ARC but are not part of its internal workflow. Figure 3 illustrates ARC’s core operation, which converts predictions into final ratings. Using protected attributes

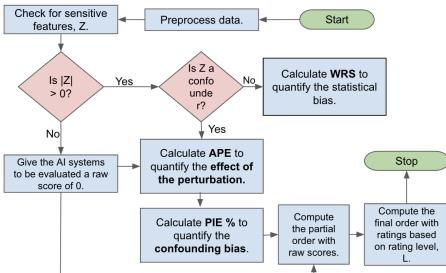


Figure 3: Predictions-to-ratings workflow showing how ARC processes predictions to compute metrics, raw scores, and final ratings.

Tasks	Data	Attributes	Models
Binary Classification	German Credit Dataset [6].	Treatment: Credit Amount (low, medium, high); Protected: Age, Gender; Outcome: Risk (good/bad).	Logistic Regression, Random
Sentiment Analysis (SAS)	EEC Dataset [12] with emotion word variations and protected attributes (Gender, Race).	Treatment: Emotion Word (positive, negative); Protected: Gender, Race; Outcome: Sentiment.	TextBlob, NR-CLex, Biased, Random
Group Recommendation	Public data from funding agencies (RFPs) and researcher profiles [32, 33].	Treatment: Request For Proposals (RFPs) and researcher profiles; Protected: Gender; Outcome: Goodness Scores (for recommended teams).	Random Matching (M0), String Matching (M1), Semantic Matching (M2), Boosted Bandit Learning (M3)
Time-series Forecasting (TSFM)	Stock prices (Mar 2023 - Apr 2024) from <i>Yahoo! Finance</i> .	Treatment: Semantic, Input-specific, and Composite perturbations; Protected: Company, Industry; Outcome: Residual.	ARIMA, Random, Biased, ViT-number-spec-large (VNS1), ViT-number-spec-small (VNS2)

Table 1: Summary of tasks that include Binary Classification, Sentiment Analysis [17], Group Recommendation [26, 34], and Time-series Forecasting [16], data attributes, AI models, and references with implementation details used in the ARC tool.

Z identified by the user, ARC computes causal metrics to answer the research questions defined in Section 2. The resulting values are aggregated into a partial order and mapped to final ratings at a chosen rating level L , allowing comparison across AI models under similar causal assumptions.

ARC implements four causal metrics in addition to standard accuracy measures. **Weighted Rejection Score (WRS)** measures

233 statistical bias by testing if outcomes differ significantly across
 234 protected groups. **Propensity Score Matching - based Impact**
 235 **Estimation (PIE%)** quantifies confounding bias by comparing the
 236 average treatment effect before and after adjustment using propen-
 237 sity score matching. For continuous treatments, the same effect can
 238 be estimated via *G-computation*, referred to as **Deconfounding**
 239 **Impact Estimation (DIE%)** in the tool. **Average Perturbation Ef-**
 240 **fect (APE)** evaluates how model outcomes vary across treatments,
 241 capturing the direct causal effect of different input variations or
 242 perturbations. **Task-specific accuracy metrics** (e.g., precision,
 243 recall, or SMAPE) complement these causal measures, allowing
 244 joint evaluation of performance and robustness.

246 3.2 Demonstration

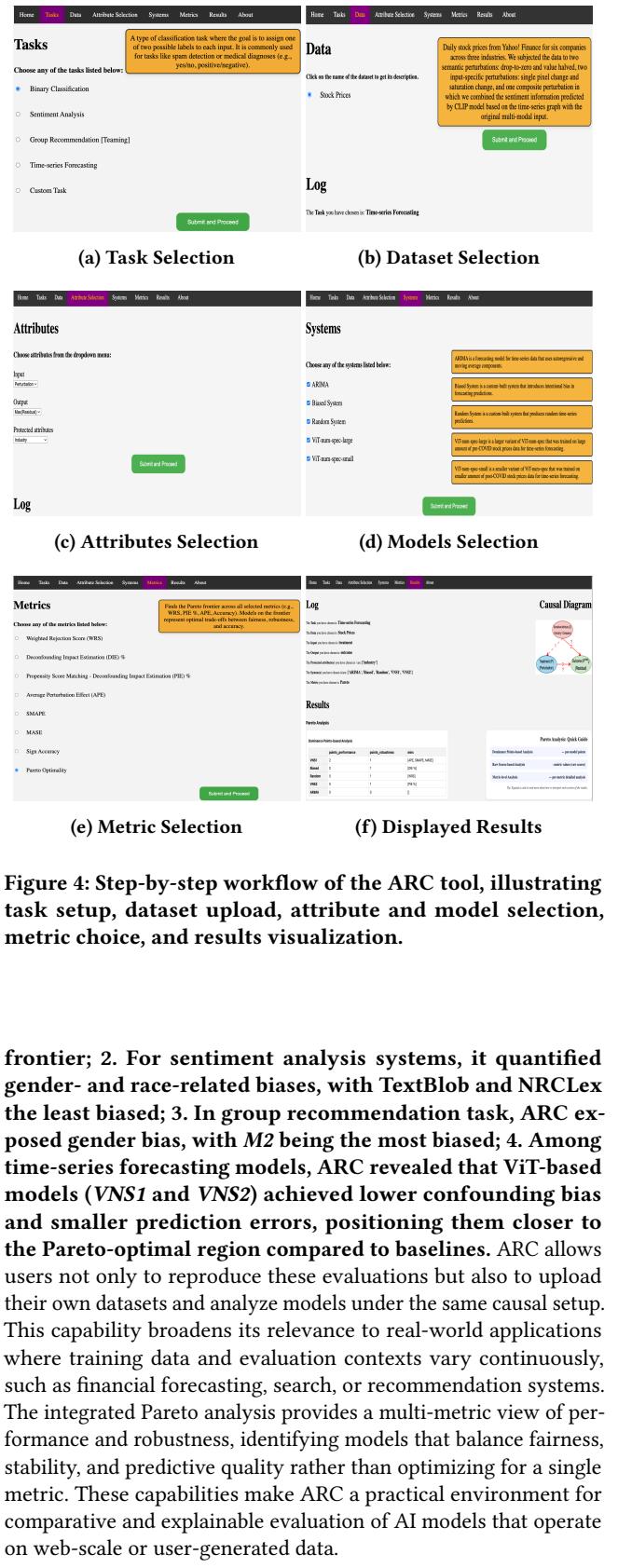
247 The ARC tool was implemented in Django. Table 1 summarizes
 248 the supported tasks, datasets, and AI models. The demonstration
 249 uses the time-series forecasting task as a running example [16].
 250 The interface allows users to select tasks, upload datasets, spec-
 251 ify attributes (*treatment* (or *input*), *outcome* (or *output*), *protected*),
 252 choose models and metrics, and view results. ARC outputs raw
 253 metric scores, final ratings, and Pareto frontier comparisons, allow-
 254 ing interactive exploration of trade-offs between robustness and
 255 accuracy within a web-based environment.

256 **1. Select a Task (Figure 4a):** The user begins by selecting a task,
 257 such as *Binary Classification*, *Sentiment Analysis*, *Group Recom-*
 258 *mendation*, *Time-Series Forecasting*, or *Custom Task*. **2. Choose a**
 259 **Dataset (Figure 4b):** The user selects a dataset relevant to the
 260 chosen task, either from pre-loaded options or by uploading their
 261 own. **3. Choose Attributes (Figure 4c):** The user specifies the
 262 *treatment* or *input*, *outcome* or *output*, and *protected attributes* that
 263 will be used in the causal analysis. **4. Select AI Models (Figure**
 264 **4d):** The user picks one or more AI models from the available op-
 265 tions for comparison. **5. Choose Evaluation Metrics (Figure 4e):**
 266 The user selects evaluation metrics defined in Section ?? that ad-
 267 dress the research questions in Section 2. The tool provides brief
 268 descriptions of each metric in an interactive popup window, as
 269 shown in Figure 4e. Complete formulations of these metrics are
 270 detailed in [16]. **6. View Results (Figure 4f):** The tool presents a
 271 structured log of user selections, computed causal results, and an
 272 accompanying causal diagram. ARC outputs both detailed scores,
 273 the robustness vs. performance trade-offs, and overall ratings for
 274 comparison across AI models within the same interface.

275 The interface shown in Figure 4 will be available for live interac-
 276 tion, allowing conference attendees to select tasks, upload sample
 277 datasets, and view resulting causal metrics and Pareto analyses in
 278 real time. The hosted version of the ARC tool will be shared at the
 279 conference venue.

281 4 Discussion

283 In this paper, we applied ARC to four diverse tasks, showing that its
 284 causal rating methodology generalizes across domains and can also
 285 be applied to user-provided datasets. ARC revealed the following
 286 key insights: **1. On the German Credit dataset, known to be**
 287 **biased with respect to gender and age [3, 18], ARC identified**
 288 **both statistical and confounding biases, with logistic regres-**
 289 **sion emerging as the most balanced model on the Pareto**



322 **Figure 4: Step-by-step workflow of the ARC tool, illustrating**
 323 **task setup, dataset upload, attribute and model selection,**
 324 **metric choice, and results visualization.**

325 **frontier; 2. For sentiment analysis systems, it quantified**
 326 **gender- and race-related biases, with TextBlob and NRCLEX**
 327 **the least biased; 3. In group recommendation task, ARC ex-**
 328 **posed gender bias, with M2 being the most biased; 4. Among**
 329 **time-series forecasting models, ARC revealed that ViT-based**
 330 **models (VNS1 and VNS2) achieved lower confounding bias**
 331 **and smaller prediction errors, positioning them closer to**
 332 **the Pareto-optimal region compared to baselines.** ARC allows
 333 users not only to reproduce these evaluations but also to upload
 334 their own datasets and analyze models under the same causal setup.
 335 This capability broadens its relevance to real-world applications
 336 where training data and evaluation contexts vary continuously,
 337 such as financial forecasting, search, or recommendation systems.
 338 The integrated Pareto analysis provides a multi-metric view of per-
 339 formance and robustness, identifying models that balance fairness,
 340 stability, and predictive quality rather than optimizing for a single
 341 metric. These capabilities make ARC a practical environment for
 342 comparative and explainable evaluation of AI models that operate
 343 on web-scale or user-generated data.

Conclusion. ARC is an extensible tool that rates AI models through a causal lens for trust and performance assessment. It combines causal reasoning with interactive evaluation to quantify robustness, encompassing fairness and stability, across both benchmark and user-supplied data. By integrating Pareto frontier, ARC helps users interpret model behavior along multiple dimensions and identify systems that achieve optimal trade-offs between robustness and accuracy. Although ARC assumes a predefined causal model, this design supports systematic investigation of well-scooped questions without requiring exhaustive causal discovery. In practice, such models can be refined using expert knowledge, controlled experiments, or causal structure learning [20]. Future work will focus on extending ARC’s causal model library, scaling its Pareto analysis for larger model families, and conducting user studies to evaluate how practitioners interpret ARC’s causal ratings [16].

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